

# The Design of a Group Key Agreement API

Giuseppe Ateniese  
Computer Science Department  
Johns Hopkins University  
*ateniese@cs.jhu.edu*

Olivier Chevassut  
Lawrence Berkeley National Laboratory  
University of California  
*chevassu@george.lbl.gov*

Damian Hasse    Yongdae Kim    Gene Tsudik\*  
Computer Networks Division  
USC Information Sciences Institute  
*{hasse,yongdaek,gts}@isi.edu*

## Abstract

*As collaborative applications grow in popularity the need for appropriate security guarantees, services and mechanisms becomes apparent. This paper describes a protocol suite and an API geared for securing collaborative applications. The API is based on the extensions of Diffie-Hellman key agreement developed in the CLIQUES project. Its core services provide authenticated group key agreement in relatively small (on the order of 100 members) dynamic peer groups.*

## 1. Introduction

Securing group communication is a complex issue. It poses a number of challenges ranging from basic cryptographic algorithms to systems, communication design and secure implementation [4]. The two common group security concerns are: 1) privacy: assuring that intra-group communication remains secret to non-members, and 2) authentication – assuring that legitimate group members can be identified as such.

The standard approach to supporting group security is based on maintaining a secret quantity known only to all current group members. The particulars of generating and distributing this secret quantity are known collectively as *group key establishment*. When the latter is achieved with one party generating a group secret, the problem is reduced to *group key distribution*. Whereas, if all group members collectively generate the group secret, the problem is referred to as *group key agreement*.

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\*Research supported by the Defense Advanced Research Project Agency, Information Technology Office (DARPA-ITO), under contract DABT63-97-C-0031.

In both cases, only current group members must have access to the group secret. We say *current* since group membership can be highly dynamic. Whenever members join or leave a group, there must be means for securely adjusting the group secret.

This paper discusses the design of an Application Programming Interface (API) for group key agreement. This API, called CLQ\_API, is based on the CLIQUES protocol suite and is geared specifically for dynamic peer groups. (Peer groups are relatively small, non-hierarchical groups typically used for replication or collaborative, many-to-many applications.) CLIQUES protocols [14, 15, 3], in turn, are the group extensions of the well-known Diffie-Hellman key exchange [6]. CLIQUES provides authenticated contributory key agreement which guarantees key independence, key confirmation, perfect forward secrecy, and resistance to known key attacks.<sup>1</sup>

CLQ\_API separates cryptographic protocols from communication, i.e., the actual group communication is left to the underlying communication subsystem (preferably, a reliable group communication system, e.g., SPREAD[2], TOTEM[11] or TRANSIS[1]). Moreover, network events such as network partitions, failures and other abnormalities are assumed to be taken care of by the same communication system. As described in subsequent sections, this allows the design of a small, concise and communication-independent API.

The rest of this paper is organized as follows. We begin with the notation and the brief description of basic operations in group key agreement. We then describe the CLIQUES protocol suite, which, in turn, consists of the following group operations: join, merge, leave and

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<sup>1</sup>For the definition of the above, the reader is referred to [10].

key refresh. Next, CLQ\_API primitives are described in detail along with some examples. Finally, we discuss the efficiency of CLQ\_API and conclude with some experimental results obtained with several popular cryptographic packages. (A more detailed description of the API is included in the Appendix.)

## 2. Group Key Agreement

The following notation is used throughout this paper:

$n$	number of protocol parties (group members)
$i, j$	indices of group members
$p, q$	prime integers
$M_i$	$i$ -th group member; $i \in [1, n]$
$G$	unique subgroup of $Z_p^*$ of order $q$
$q$	order of the algebraic group
$g$	exponentiation base; generator in group $G$
$x_i$	long-term private key of $M_i$
$N_i$	$M_i$ 's session random number $\in Z_q$
$S_n$	group shared key among $n$ members
$K_{ij}$	long-term shared secret between $M_i$ and $M_j$
$ a $	bit length of integer $a$
$H$	output size of hash function
$inv(a, b)$	multiplicative inverse of $a$ modulo $b$

### 2.1. Group key agreement operations

A comprehensive group key agreement API must handle adjustments to the group secret(s) stemming from single- and multiple-member membership population changes. This section describes the purpose of each of these operations.

**Single-member changes:** include single member additions or deletions. The former occurs when a prospective member wants to join a group and the latter – when a member wants to leave (or is forced to leave) a group. Both operations may be performed by the group controller(s) or by consent of all group members, depending on the local policy.

**Multiple-member changes:** also include addition and deletion. The former can be further broken into:

- Mass join: multiple disparate new members are brought into an existing group
- Group fusion: two or more groups are merged to form a single group.

The latter includes:

- Mass leave: multiple members must be removed at the same time.
- Group fission: a monolithic group needs to be broken into smaller groups.

**Key refresh:** is not a membership change operation, however, we discuss it here for the sake of completeness. It has two main purposes:

- Limit the amount of ciphertext generated with the same key.  
Since it is easier to perform cryptanalysis with more ciphertext/plaintext pairs, a routine group key refresh operation is needed. The lifetime of a key is determined by the application-specific policy.
- Recover from the compromise of a current group secret or a member's contribution. (We note that a compromise of a member's contribution can result in disclosure of all group secrets contributed to by this member. Therefore, not only the group shared keys, but also the individual key shares must be periodically refreshed.)

## 3. CLIQUES Protocols

As mentioned above, CLIQUES is a protocol suite providing authenticated contributory key agreement for dynamic peer groups. The following operations are supported by CLIQUES:

- Join: a new member is added to the group.
- Merge: one or more members are added to the group.
- Leave: one or more members are removed from (or leave) the group.
- Key Refresh: generates a new group shared key.

Each operation is discussed in the remainder of this section. The mapping between the group membership changes and the corresponding key agreement (cryptographic) operations is as follows:

Membership Operation	CLIQUES Operation
Forced leave	Leave
Voluntary leave	Leave
Single join	Join
Mass join	Merge
Group fusion	Merge
Group fission	Leave
Mass leave	Leave
Key refresh	Key Refresh

### 3.1. Group Controller and Group Key

**Group Controller.** In the current version of CLIQUES, the last member to join the group becomes a *group controller*. Equivalently, the role of a group controller is always played by the newest member. This behavior can be easily changed if required. In fact, any selection criteria can be used to select a group controller as long as it yields a consistent outcome across all group members. (CLIQUES assumes that the underlying communication system provides a timely and consistent membership view to all group members; this property is referred to as *membership view synchrony*.) One obvious alternative to the present criterion is to let the oldest member be the group controller.

We emphasize that a group controller is not in any way a privileged group member. It exists to prevent contention and should be viewed as a burden (or a chore) rather than a privilege. Specifically, the group controller assists new members in joining the group and initiates operations stemming from departing members or the need for periodic re-keying.

Furthermore, it is important to note that *any* group member can, at any time, initiate a group re-key by unilaterally updating its key share and distributing appropriate partial keys to the rest for the group<sup>2</sup>. (See below.)

**Group Key.** In the following operations, the group key (also referred to as group secret) has the form  $S_n = g^{N_1 \cdots N_i \cdots N_n}$ , where  $n$  is the group size and  $N_i$  ( $0 < i \leq n$ ) is provided by the  $i$ -th member,  $M_i$ [14]. In all CLIQUES protocols, the last broadcast message is always the set formed by:

$$g^{K_{in} \frac{N_1 \cdots N_n}{N_i}} \quad \forall i \in [1, n-1]$$

This set, from the last broadcast, must be retained by each group member. This is necessary since any member can become a controller due to a group partition or a network fault. (In other words, a non-controller can

<sup>2</sup>Though we fully support re-keying mechanism, its usage depends on local policy.

become a group controller if all “younger” members fail or become partitioned out.) Although the entire group receives this message from the current controller, each member uses a different element (key) to compute the new group secret.

Finally, the computation of the pairwise long-term key,  $K_{ij}$ , shared between any two members  $M_i$  and  $M_j$  is assumed to be performed before its use is required in the protocol.

### 3.2. Join

The join operation adds a new member,  $M_{n+1}$ , to the current group of  $n$  members. During this process a new group shared key,  $S_{n+1}$ , is computed and  $M_{n+1}$  becomes the new group controller. Assuming that  $M_n$  is the current controller, the protocol runs as follows:

1.  $M_n$  generates a new secret and random exponent  $N'_n$  and produces the following set:<sup>3</sup>

$$\mathcal{M} = \{g^{N_1 \cdots N'_n / N_i} \mid i \in [1, n-1]\}$$

Next,  $\mathcal{M}$  is sent to  $M_{n+1}$ .

2. Upon receipt of the message,  $M_{n+1}$  generates a new secret exponent  $N_{n+1}$  and computes:

$$\mathcal{M}' = \{g^{K_{i,n+1} N_1 \cdots N'_n N_{n+1} / N_i} \mid i \in [1, n]\}$$

This set is broadcast to the entire group (including itself).

3. Upon receipt of the broadcast, each  $M_i$  computes the shared group key as follows:

$$\left(g^{\frac{N_1 \cdots N'_n N_{n+1}}{N_i} \cdot K_{i,n+1}}\right)^{K_{i,n+1}^{-1} \cdot N_i} = g^{N_1 \cdots N'_n N_{n+1}} = S_{n+1}$$

Steps 1 and 2 require  $n$  modular exponentiations (by  $M_n$  and  $M_{n+1}$ , respectively) and step 3 requires a single exponentiation by each member. Hence, the protocol requires  $(2n+1)$  serial exponentiations.

### 3.3. Merge

The merge operation adds  $k > 0$  members to the current group of  $n \geq 1$  members. Let  $m = n + k$ . During this process a new group shared key,  $S_m$ , is computed and  $M_m$  becomes the new group controller. Assuming  $M_n$  is the current controller, the protocol runs as follows:

<sup>3</sup>This is achieved by exponentiating  $N'_n * inv(K_{in}, p) * inv(N_n, q)$  to each element in the last broadcast message.

1.  $M_n$  generates a new exponent  $N'_n$  and computes:  $g^{N_1 \dots N_{n-1} N'_n}$  by modular exponentiation of the previous group shared key with  $(N'_n * inv(N_n, q))$ . Then, this value is sent to  $M_{n+1}$ , the first new member.
2. Each new (merging) member  $M_j$ ,  $j = n + 1, \dots, m - 1$ , generates a new exponent  $N_j$ , computes  $g^{N_1 \dots N'_n \dots N_j}$  and forwards the result to  $M_{j+1}$ .
3. Upon receipt of the accumulated value,  $M_m$  simply broadcasts it to the entire group.
4. Every group member  $M_i$  (old and new) received the broadcast, computes  $g^{N_1 \dots N'_n \dots N_{m-1} / N_i}$  and sends back to  $M_m$ .
5. Having received all responses from the group members,  $M_m$  generates a new secret exponent  $N_m$  and produces the following set: <sup>4</sup>

$$\mathcal{M} = \{g^{K_{im} N_1 \dots N'_n \dots N_m / N_i} \mid i \in [1, m - 1]\}$$

which it broadcasts to the group.

6. Each member  $M_i$  computes the group shared key exactly as in the last step of the Join protocol.

In case of a single-member Merge ( $k = 1$ ), step 2 is not required and the rest of the protocol runs as above.

Steps 1 and 2 require a total of  $k$  modular exponentiations while steps 4 and 6 each involve one exponentiation (in parallel by each member). Finally, step 5 needs  $(n + k - 1)$  exponentiations. Thus the total number of serial exponentiation for a  $k$ -member Merge is  $(n + 2k + 1)$ .

### 3.4. Leave

The leave operation removes one or more members from the group of  $n$  members. As a result, a new group shared key  $S_{n-k}$ , is computed where  $k$  is the number of the departing members. Let the set  $\mathcal{K}$  denote the leaving members.

There are two cases to consider: 1) the current controller  $M_n \in \mathcal{K}$  and 2)  $M_n \notin \mathcal{K}$ . In the first case, the controller's role is passed on to the most recent remaining member  $M_d$  where  $d = n - k$ . (See Section 4.1 below.) Assuming that members are indexed in the order of joining the group (i.e.,  $M_n$  is the most recent member to join) the remaining members must be *renumbered* after a Leave. Now, even if the previous

<sup>4</sup>Note that  $\mathcal{M}$  is the same as its counterpart in the Join protocol.

controller is not in  $\mathcal{K}$ , it will acquire a new index and become  $M_d$  due to renumbering.

The protocol runs as follows:

1. The controller  $M_d$  generates a new exponent  $N'_d$ , produces the following set and broadcasts it to the remaining group.

$$\mathcal{M} = \{g^{K_{i,d} N_1 \dots N'_d / N_i} \mid M_i \notin \mathcal{K}\}$$

2. Having received  $\mathcal{M}$ , each  $M_i$  computes:

$$S_d = (g^{\frac{N_1 \dots N'_d}{N_i} \cdot K_{i,d}})^{K_{i,d}^{-1} \cdot N_i} = g^{N_1 \dots N_d}$$

Members of the departing set  $\mathcal{K}$  cannot compute the new key since the group controller only computes partial keys for the remaining group.

Step 1 requires  $n - k$  exponentiations whereas step 2 needs a single exponentiation by each member. In total, the leave operation requires  $(n - k + 1)$  serial exponentiations.

### 3.5. Key refresh

The key refresh operation updates the current group shared key,  $S_n$ . It is, in fact, a special case of a Leave with  $k = 0$ . Its usage depends on the application policy.

## 4. CLQ\_API

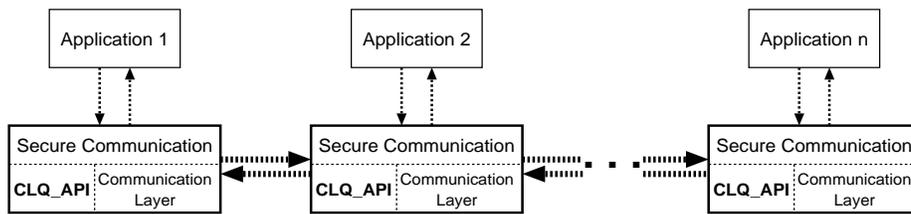
CLQ\_API is a group key management API based on the CLIQUES protocol suite. It is fairly small, containing only eight function calls.

CLQ\_API does not perform any communication. All API calls either accept a token, produce one or both. As mentioned before, CLIQUES (and CLQ\_API) requires reliably and sequenced communication and membership view synchrony. Any communication system providing these features can be used in conjunction with CLQ\_API, e.g., SPREAD, TOTEM, and TRANSIS might be used.

### 4.1. CLQ\_API Calls

This section describes CLQ\_API calls. Each call represents one or more steps in one of the group operations presented in Section 3. Details of the data structures, definitions and secondary function calls can be found in the appendix.

The following terms are used throughout this section:



**Figure 1. Communication layer and CLQ\_API**

Context: contains information about each user required by CLQ\_API.

Epoch: message sequence number of a token. It is used to keep track of the group secret evolution and to prevent replay attacks.

Timestamp: time when a token is sent. It is used to check the freshness of an incoming token.

Session random: secret key share generated by each member.

Token: basic protocol unit; includes: epoch, timestamp, and a CLIQUES protocol message.

We now describe the CLQ\_API calls:

- `clq_proc_join`: performs *step 1* of the join operation. The controller calls this function to hand over information about the current group to a new member who will eventually become the new controller. The purposes of this function are:
  - generate a new session random for the current controller.
  - remove long term keys and previous session random from the partial keys of all users.
  - add the new session random into the partial keys of all users.
- `clq_join`: performs *step 2* of the join operation. The new group member calls this function using the token received from the current controller. The purposes of this function are:
  - generate a new session random for the new member.
  - generate long-term keys between the new member and each user (can also be done before calling this function).
  - compute the partial keys for other group members.
- `clq_update_ctx`: performs the *last step* of the join, merge, leave, and key refresh operation. Every member calls this function in order to update the group shared key upon receipt of the token sent by the current controller. The main purpose of this function is to compute group shared key with the caller's session random and the incoming token.
- `clq_update_key`: performs *step 1 and 2* of the merge operation. This function is called by the current controller and by all (but last) of the new members to add their session randoms to the group shared key.
 

The main purposes of this function are:

  - generate new session random.
  - add new session random to the group shared key.
- `clq_factor_out`: performs *step 4* of the merge operation. Every group member (except the controller) calls this function to factor out its own session random number from the group shared key.
- `clq_merge`: performs *step 5* of the merge operation. The last new member (new controller) calls this function to add its session random to each of received partial keys from the group members.
- `clq_leave`: performs *step 1* of the leave operation. Every group member calls this function right immediately after one or more members leave the group. A group member may also become the current controller after calling this function; this can happen if it finds itself to be the newest member within the remaining group. The main purpose of this function is to remove the information of the leaving members. If the controller calls this function, then two more steps need to be performed:
  - generate new session random.
  - compute partial keys for other group members (except, of course, the departed ones).

- `clq_refresh_key`: performs *step 1* of the key refresh operation. The current controller calls this function, when the group shared key needs to be updated. The main purposes of this function are:
  - To generate new session random number.
  - To compute new partial keys by adding this session random number and removing old one.

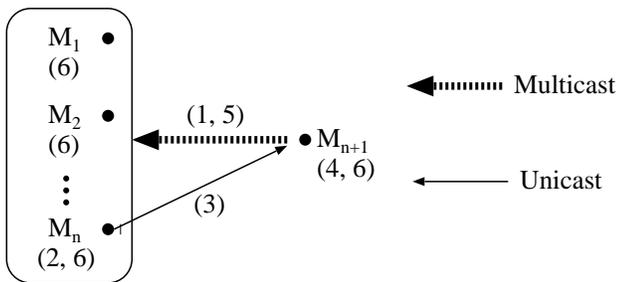
## 4.2. Operations of CLQ\_API

Before we explain each of the group operations in the API, we need to define some message types:

- `NEW_MEMBER` : sent by the controller to a new member, when a new member joins the group.
- `KEY_UPDATE_MESSAGE` : sent to every member in order to update the group shared key.
- `MERGE_KEY_UPDATE` : sent to every member to update the group shared key in merge operation.
- `MERGE_BROADCAST` : broadcast from the last new member when one or more members merge.
- `MERGE_FACTOR_OUT` : sent by each group member to the new controller in a merge operation.
- `MASS_JOIN` : sent to the next new member in a merge operation.

We now clarify group operations using the function calls from the previous section.

- Join

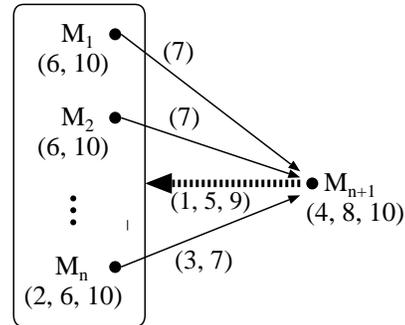


**Figure 2. Join operation**

- (1) New member  $M_{n+1}$  calls communication protocol JOIN primitive.

- (2) The current controller calls `clq_proc.join` to generate a token containing `NEW_MEMBER` message.
- (3) The token is sent to the new member.
- (4) The new member calls `clq_join` to generate a token containing `KEY_UPDATE_MESSAGE`.
- (5) The token is broadcast to the entire group.
- (6) Every user calls `clq_update_ctx` to compute the new group shared key.

- Merge (single member)



**Figure 3. Merge operation**

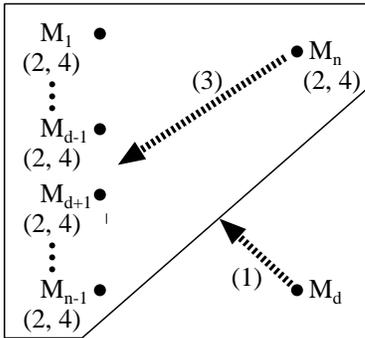
- (1) New member  $M_{n+1}$  calls communication protocol JOIN primitive.
- (2) The current controller calls `clq_update_key` to generate a token containing `MASS_JOIN` message.
- (3) The token is sent to the new user (who becomes the new controller).
- (4) The new controller calls `clq_update_key` to generate a token containing `MERGE_BROADCAST` message.
- (5) The token is broadcast to the group.
- (6) Each member (except the new one) calls `clq_factor_out` to generate a token containing `MERGE_FACTOR_OUT` message.
- (7) Each member sends the output token back to the new controller.
- (8) For each received token, the new controller calls `clq_merge` to generate a token containing `MERGE_KEY_UPDATE` message. When the last token is received, `MERGE_KEY_UPDATE` returns an output token.

- (9) The token is broadcasted to the entire group.
- (10) Every user calls `clq_update_ctx` to compute the new group shared key.

- Merge (multiple members)

- (1) A MERGE event occurs either at an explicit request or as a result of a multiple members calling communication protocol `join` to join a group.
- (2) The current group controller calls `clq_update_key` to generate a token containing MASS\_JOIN message.
- (3) The token is sent to the first merging member.
- (4) Upon reception of the token, the next user calls `clq_update_key` to generate a token containing MASS\_JOIN message.
- (5) The token is sent to the next new member.
- (6) Upon reception of the token, the last user calls `clq_update_key` to generate a token containing MERGE\_BROADCAST message.
- (7) The token is broadcasted to the entire group.
- (8) Upon reception of the message, each member except the last one calls `clq_factor_out` to generate a token containing MERGE\_FACTOR\_OUT message.
- (9) The token is sent back to the last new user.
- (10) For each output token, the last new member calls `clq_merge` to generate a token containing MERGE\_KEY\_UPDATE.
- (11) The token is broadcasted to the entire group.
- (12) Every user calls `clq_update_ctx` to compute the new group shared key.

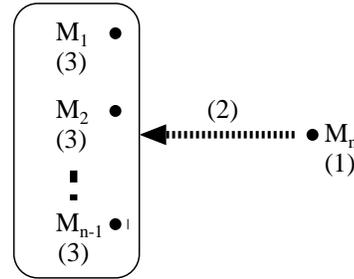
- Leave



**Figure 5. Leave operation**

- (1) The leaving member  $M_d$  calls communication protocol LEAVE primitive. (In case of a member disconnect or network failure the communication system notifies the group of the event.)
- (2) All group members call `clq_leave`; only the group controller obtains the output token containing KEY\_UPDATE\_MESSAGE.
- (3) The token is broadcast to the entire group.
- (4) Upon reception of the token, every user calls `clq_update_ctx` to compute the new group shared key.

- Key refresh



**Figure 6. Key refresh operation**

- (1) The controller calls `clq_refresh_key` to generate a token containing KEY\_UPDATE\_MESSAGE.
- (2) The token is broadcasted to the entire group.
- (3) Upon reception of the token, every user calls `clq_update_ctx` to compute the new group shared key.

## 5. Efficiency

The communication overhead is summarized in Table 1.

Table 2 illustrates computation costs. Exponentiation is the most expensive operation as it requires  $O(\log^3 p)$  bit operations in  $Z_p^*$ . Given  $a$  and  $p$ , finding the inverse of  $a \in Z_p^*$  requires only  $O(\log^2 p)$  bit operations (using the extended Euclidean algorithm). Similarly, the multiplication of  $a$  and  $b$  modulo  $p$  requires  $O(\log^2 p)$  bit operations. See [9, 10] for more details. Hence, the speed of each operation depends largely on the number of serial exponentiations. (Note that the cost for generating the long term keys is not included in this table.)

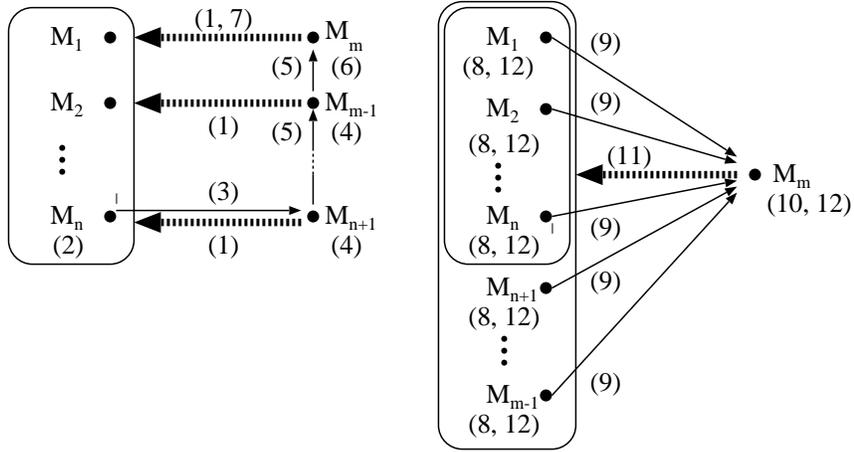


Figure 4. Merge(several members) operation

Table 1. Communication costs

Operations	Join	Merge	Leave	Refresh	k-Merge	k-Leave
Number of users after operation	$n+1$	$n+1$	$n-1$	$n$	$n+k$	$n-k$
Rounds	2	3	1	1	$k+2$	1
Broadcasts	1	2	1	1	2	1
Reverse broadcast	0	1	0	0	1	0
Total messages	2	$n+2$	1	1	$n+2k$	1
Maximum bandwidth	$n$	$n$	$n-1$	$n-1$	$n+k-1$	$n-k$

Table 2. Computation costs

Operations	Join	Merge	Leave	Refresh	k-Merge	k-Leave
Number of users after operation	$n+1$	$n+1$	$n-1$	$n$	$n+k$	$n-k$
Serial exponentiation	$2n+1$	$n+3$	$n-1$	$n$	$n+2k+1$	$n-k$
Total exponentiation	$3n+2$	$3n+2$	$2n-3$	$2n-1$	$3n+4k-2$	$2n-2k-1$

## 5.1. Exponentiation

As mentioned earlier, modular exponentiation is most expensive operation in CLIQUES protocols. In this section, we compare the performance of modular exponentiation operations using three different cryptographic libraries on three different processors(See Table 3).

The cryptographic libraries are summarized as follows:

- RSAREF[13]  
A cryptographic toolkit for privacy-enhanced mail. We used version 2.0 developed in 1996.
- Crypto++[5]  
A public domain C++ class library of cryptographic schemes published by Wei Dai. Note that, since addition and subtraction are implemented for the Pentium assembler, this package performs better on Pentium than in other microprocessors. We used version 3.1 developed in May 1999.
- OpenSSL[12]  
A successor of SSLeay[8], OpenSSL is a cryptographic toolkit implementing Secure Socket Layer(SSL v.2/3)[7]. (Implements some basic operations in assembler on various platforms.) We used version 0.9.3a developed in May 1999.

We measured the performance of modular exponentiation  $y = g^x \pmod{p}$ , where  $p$  is a random 512-bit prime,  $g$  a 512-bit generator for  $\text{GF}(p)$  of order  $q$ (160 bit), and  $x$  a random 160 bit integer. Table 4 shows the comparison.

At the time of this writing, OpenSSL appears to be the fastest of all public domain cryptographic libraries. On a Pentium II processor it requires only 2.5 msec for each 512-bit modular exponentiation.

## 6. Conclusion

This paper describes a protocol suite and an API designed specifically for securing dynamic collaborative applications in unreliable networks. The API is based on the extensions of Diffie-Hellman key agreement developed in the CLIQUES project. It provides core security services (most notably, authenticated key agreement) for relatively small and dynamic peer groups.

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## Appendix: Data Structures and Definitions of CLQ\_API

- CLQ\_CONTEXT
  - Type : Structure
  - Description : This structure contains the context of a member,  $M_i$ , in a specific group.
  - Contents
    - \* member\_name (String): Name of the user  $M_i$
    - \* group\_name (String): Name of the group

**Table 3. Target platform**

Machine	CPU speed	Main memory	OS	Compiler
Ultra Sparc I	233 MHz	64 MB	SUN OS 5.5.1	gcc 2.7.2.2
Pentium I	233 MHz	48 MB	Linux 2.0.36	gcc 2.7.2.3
Pentium II	450 MHz	256 MB	Linux 2.2.9	egcs 1.1.2

**Table 4. Comparison results**

Machine	OpenSSL	Crypto++	RSAREF
UltraSparc I	16.6 msec	60.2 msec	146.3 msec
Pentium I	6.4 msec	N/A	N/A
Pentium II	2.5 msec	7.6 msec	22.2 msec

- \* `key_share` ( $|q|$  bit integer):  $M_i$ 's session random number,  $N_i$
  - \* `group_secret` ( $|p|$  bit integer): Current group shared key
  - \* `group_secret_hash` ( $H$  bit integer): Hash of `group_secret`
  - \* `group_members_list` (CLQ\_GML): List of current group members
  - \* `first` (Pointer): Pointer to the first member in the `group_members_list`
  - \* `last` (Pointer): Pointer to the last member in the `group_members_list`
  - \* `me` (Pointer): Pointer to the member  $M_i$  in the `group_members_list`
  - \* `params` (CLQ\_PARAM): Diffie-Hellman parameters
  - \* `key` (CLQ\_KEY): Private and public key of  $M_n$
  - \* `epoch` (Integer): Last message number used
- CLQ\_GML
    - Type : Double linked list of CLQ\_GM data structure
    - Description : This structure is a node of the `group_member_list`.
    - Contents
      - \* `member` (CLQ\_GM): The current group member
      - \* `prev` (Pointer): Pointer to the previous node in the list
      - \* `next` (Pointer): Pointer to the next node in the list
  - CLQ\_GM
    - Type : Structure
    - Description : This structure contains information about a specific member.
- Contents
    - \* `member_name` (String): Name of the member
    - \* `long_term_key` ( $|p|$  bit integer): Long term shared key between myself and `member_name`, i.e.  $K_{ij}$  where  $i$  is related to the public key of `member_name`, and  $j$  to my private key
    - \* `last_partial_key` ( $|p|$  bit integer): Last partial key for `member_name`.
  - CLQ\_TOKEN
    - Type : Structure
    - Description : Communication token used by CLQ\_API, see also CLQ\_TOKEN\_INFO
    - Contents
      - \* `length` (Integer): Size of `t_data`
      - \* `t_data` (Integer array): Contains the following encoded data: `group_name`, `message_type`, `time_stamp`, `sender_name`, `epoch`, `group_members_list` (without `long_term_key`)
  - CLQ\_TOKEN\_INFO
    - Type : Structure
    - Description : This structure contains information about the token.
    - Contents
      - \* `group_name` (String): Name of the group
      - \* `message_type` (MSG\_TYPE): Type of the message
      - \* `time_stamp` (Integer): Time stamp of the message
      - \* `sender_name` (String): Name of the sender
  - CLQ\_PARAM
    - Type : Structure

- Description : Diffie-Hellman, DH, public parameters, i.e.  $p$ ,  $q$  and  $g$
- Contents
  - \*  $p$  ( $|p|$  bit integer): DH parameter  $p$
  - \*  $q$  ( $|q|$  bit integer): DH parameter  $q$
  - \*  $g$  ( $|p|$  bit integer): DH parameter  $g$
- CLQ\_KEY
  - Type : Structure
  - Description : Public key and private key of the user
  - Contents
    - \* `priv_key` ( $|q|$  bit integer): Private key of the user
    - \* `pub_key` ( $|p|$  bit integer): Public key of the user

## Appendix: API Calls of CLQ\_API

- `clq_join(ctx, member_name, group_name, input_token, output_token)`
  - Caller : New member
  - Related to : Join
  - Parameters
    - \* `ctx` (CLQ\_CONTEXT) : Context for the new user, this should be created in this function.
    - \* `member_name` (String): Name of the user calling this function
    - \* `group_name` (String) : Name of the group that has been joined. This name has to match with the one that is included in the `input_token`.
    - \* `input_token` (CLQ\_TOKEN): Message received from the controller. It is the `output_token` generated by `clq_proc_join`.
    - \* `output_token` (CLQ\_TOKEN): New key update message to be broadcasted to the group. It will be used as `input_token` of `clq_update_ctx`.
- `clq_proc_join(ctx, member_name, output_token)`
  - Caller : Current controller
  - Related to : Join
  - Parameters
    - \* `ctx` (CLQ\_CONTEXT): Current group context, `ctx` will be modified only if the caller is the controller.
    - \* `member_name` (String): Name of the new member
    - \* `output_token` (CLQ\_TOKEN): This token should be used as the `input_token` for `clq_join`.

- `clq_update_ctx(ctx, input_token)`
  - Caller : Every group member.
  - Related to : Join, Merge, Leave, Key Refresh
  - Parameters
    - \* `ctx` (CLQ\_CONTEXT): Current context of each member
    - \* `input_token` (CLQ\_TOKEN): Generated by new member or by the current controller, when an update of key is required(i.e. a user join, a user left, or the key has been compromised). It should be the `output_token` of `clq_join`, `clq_merge`, `clq_leave`, or `clq_refresh`.
- `clq_update_key(ctx, member_list, input_token, output_token)`
  - Caller : Current or new controller.
  - Related to : Merge
  - Parameters
    - \* `ctx` (CLQ\_CONTEXT): Current group context
    - \* `member_list` (List of string): List of names of the new members. When a new member calls this function, this list should be null(Since the `input_token` is valid).
    - \* `input_token` (CLQ\_TOKEN): Output of `clq_update_key` by the current controller or previous new member. When the controller calls this function, `input_token` should be null. (Since the `member_list` is valid).
    - \* `output_token` (CLQ\_TOKEN): Contains refreshed `group_secret`. It will be used as `input_token` of
      - `clq_factor_out` by the current group members or
      - `clq_update_key` by the next new member.
- `clq_factor_out(ctx, input_token, output_token)`
  - Caller : Every group member (except the last one<sup>5</sup>)
  - Related to : Merge
  - Parameters
    - \* `ctx` (CLQ\_CONTEXT): Current member context
    - \* `input_token` (CLQ\_TOKEN): `output_token` of `clq_update_key`
    - \* `output_token` (CLQ\_TOKEN): Contains updated `last_partial_key` by removing each user's `key_share`. It will be used as `input_token` of `clq_merge`.

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<sup>5</sup>If the current controller, i.e. the last member, calls `clq_factor_out` then the `output_token` will return NULL

- `clq_merge(ctx, sender_name, input_token, output_token)`
  - Caller : The last new member
  - Related to : Merge, Mass Join
  - Parameters
    - \* `ctx (CLQ_CONTEXT)`: Current group context. `ctx` will be modified.
    - \* `sender_name (String)`: Name of the sender of the `input_token`
    - \* `input_token (CLQ_TOKEN)`: `output_token` of `clq_factor_out`
    - \* `output_token (CLQ_TOKEN)`: Contains updated `last_partial_key`
- `clq_leave(ctx, member_list, output_token)`
  - Caller : Every group member
  - Related to : Leave
  - Parameters
    - \* `ctx (CLQ_CONTEXT)`: Current group context
    - \* `member_list (List of string)`: List of members leaving
    - \* `output_token (CLQ_TOKEN)`: Updated message to be broadcasted to the group
- `clq_refresh_key(ctx, output_token)`
  - Caller : Controller
  - Related to : Key Refresh
  - Parameters
    - \* `ctx (CLQ_CONTEXT)`: Current group context. `ctx` will be modified.
    - \* `output_token (CLQ_TOKEN)`: Updated message to be broadcasted to the group
- `clq_destroy_ctx(ctx)`
  - Description : Frees the space occupied by the current context
  - Parameters
    - \* `ctx (CLQ_CONTEXT)`: Current group context. `ctx` will be destroyed.
- `clq_destroy_token(token)`
  - Description : Frees the space occupied by the token
  - Parameters
    - \* `token (CLQ_TOKEN)`: Input or `output_token`
- `clq_first_user(ctx, member_name, group_name)`
  - Description : `clq_first_user` is called by the first user who joins a group
  - Main purposes
    - \* Generates `key_share`.
    - \* Generates member context.
- `clq_join(ctx, member_name, group_name)`
  - Caller : The first member in a group
  - Related to : Join
  - Parameters
    - \* `ctx (CLQ_CONTEXT)`: Current member context. `ctx` should be created.
    - \* `member_name (String)`: Name of the first user
    - \* `group_name (String)`: Name of the group